









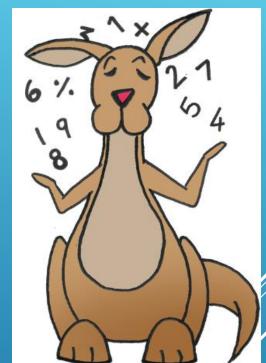


# PROGRESSION IN MATHEMATICS AND NUMERACY: LLANRHIDIAN PRIMARY SCHOOL

Policy and Practice at Llanrhidian Primary School

In Llanrhidian, we encourage pupils to explore links with mathematics and numeracy across all areas of learning and in the real world. Embedded provision to develop the appropriate skills and knowledge and experiences for Mathematics and Numeracy includes:

- Chunky mathematics spotlight lessons.
- Numeracy links in IQ tasks
- Numeracy intervention for identified pupils
- Chilli Challenges
- TTRS (online platforms)
- Weekly Chilli Assessments
- The concrete to visual to abstract approach
- Numicon and Target Maths
- Plus 1 and Plus 2 interventions
- Flip learning lessons and resources available digitally

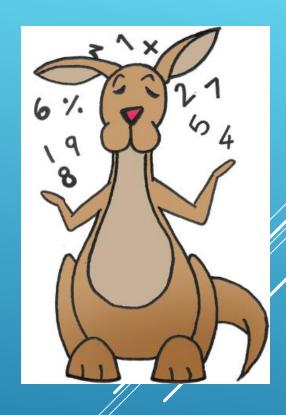


This policy has been produced to ensure consistency and progression in teaching throughout the school. It aims to give an overview of the key steps that can be made from concrete, to pictorial, to abstract recording strategies and how they can be taught in any year group. The policy aims to identify the progression for each pupil

**OVERALL AIM OF THE POLICY** 

The overall aim is that when our pupils leave Llanrhidian, they:

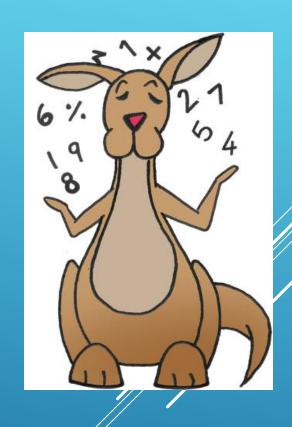
- have a secure knowledge of number facts and a confident understanding of the four operations.
- can transfer mathematical skills to a variety of contexts and everyday situations and can identify the appropriate steps and information needed to complete a task or reach a solution.
- are able to use their schema and understanding to carry out calculations mentally and be able to apply appropriate strategies when using larger numbers.
- have an efficient, reliable method for calculation of each operation that pupils can apply with confidence when undertaking calculations that they cannot carry out mentally.



#### **OVERALL AIM FOR THE PUPILS**

Each classroom will be resourced with materials to support the delivery of Maths; such items might include number lines, multiplication tables, 100 squares, 2D and 3D shapes, multilink cubes, dice and other smaller items.

Our pupils should be encouraged to use whatever resources are available to them in the classroom and which they feel would be beneficial to help them when completing Maths work.





We have got a range of resources to support our learners to consolidate the 4 main operations.

- All classes have links to numeracy websites on their class web pages that are age appropriate and support the learning needs of the pupils
- Pod Pila Pala launch the Numicon scheme to support the concrete learning of the 4 operations. This resource then carries on through the school as and when required to support all learners.
- Pod Pila Pala and Pengwin have Numbots through J2E in HWB for tailored maths games. This can also be accessed by all pupils if it is still deemed as an appropriate support resource
- From Pod Pysgodyn onwards pupils have access to Times Table Rock Stars (TTRS) which is a great online platform for practising and learning rapid recall of your times table and division facts.
- KS2 class pages have links to bar modelling strategies to help visual learners practise reasoning problems that involve the 4 operations using pictorial methods
- The whole school has access to the Plus of 1 and Plus of 2 scheme available to them that has lesson ideas and resources for the 4 operations for each year group across a full academic year



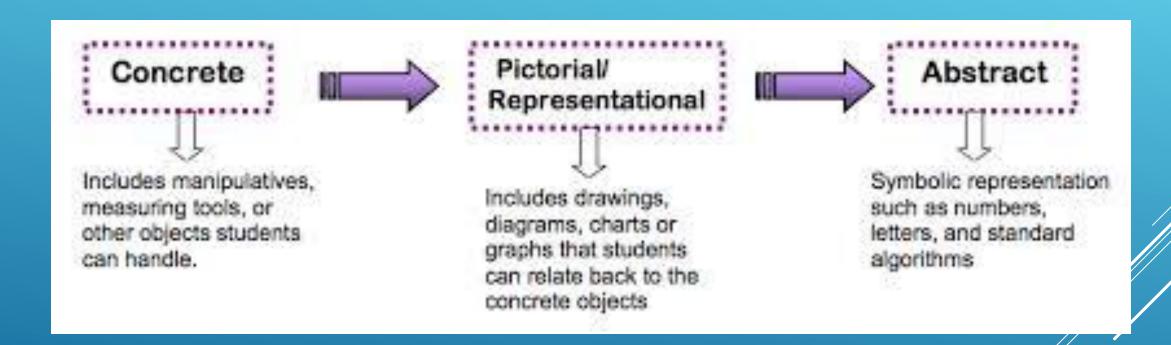
#### **RESOURCES TO SUPPORT**

The model of progression is based on the develop of five interdependent proficiencies, outlines below. This model of progression can be considered as both longitudinal and cross-sectional. To ensure progress in any mathematics learning, proficiencies should be developed and connected in time and should also develop over time.

- Conceptual understanding.
- Communication using symbols
- Fluency
- Logical reasoning
- Strategic competence.
- Principles of Progression

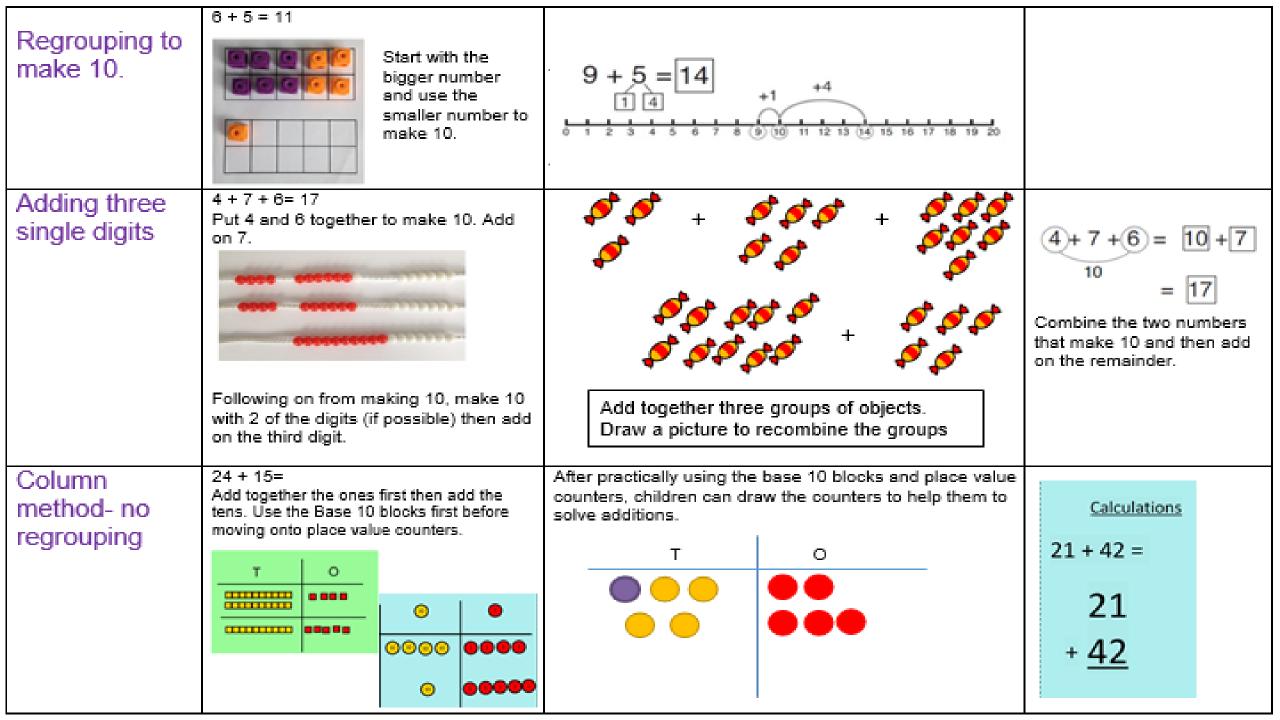


At Llanrhidian, we recognise the importance of building on pupil's prior knowledge (their schema) to help them make maximum progress in the subject. So, when it comes to the journey from concrete, to pictorial, to abstract, we are consistent in our approach.



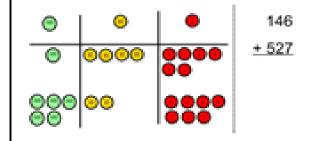
#### CONCRETE, PICTORIAL TO ABSTRACT APPROACH

<u>Addition</u>			
Objective and Strategies	Concrete	Pictorial	Abstract
Combining two parts to make a whole: part-whole model	Use cubes to add two numbers together as a group or in a bar.	Use pictures to add two numbers together as a group or in a bar.	4 + 3 = 7  10= 6 + 4  Use the part-part whole diagram as shown above to move into the abstract.
Starting at the bigger number and counting on	Start with the larger number on the bead string and then count on to the smaller number 1 by 1 to find the answer.	12 + 5 = 17   The start at the larger number on the number line and count on in ones or in one jump to find the answer.	5 + 12 = 17  Place the larger number in your head and count on the smaller number to find your answer.
Regrouping to make 10.		Use pictures or a number line. Regroup or partition the smaller number to make 10.	7 + 4= 11 If I am at seven, how many more do I need to make 10. How many more do I add on now?

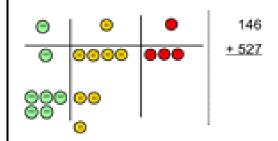


Column methodregrouping

Make both numbers on a place value grid.



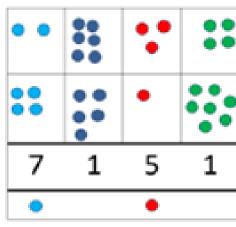
Add up the units and exchange 10 ones for one 10.



Add up the rest of the columns, exchanging the 10 counters from one column for the next place value column until every column has been added.

This can also be done with Base 10 to help children clearly see that 10 ones equal 1 ten and 10 tens equal 100.

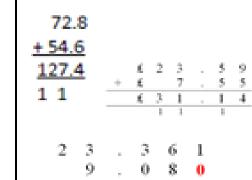
As children move on to decimals, money and decimal place value counters can be used to support learning. Children can draw a pictoral representation of the columns and place value counters to further support their learning and understanding.



Start by partitioning the numbers before moving on to clearly show the exchange below the addition.

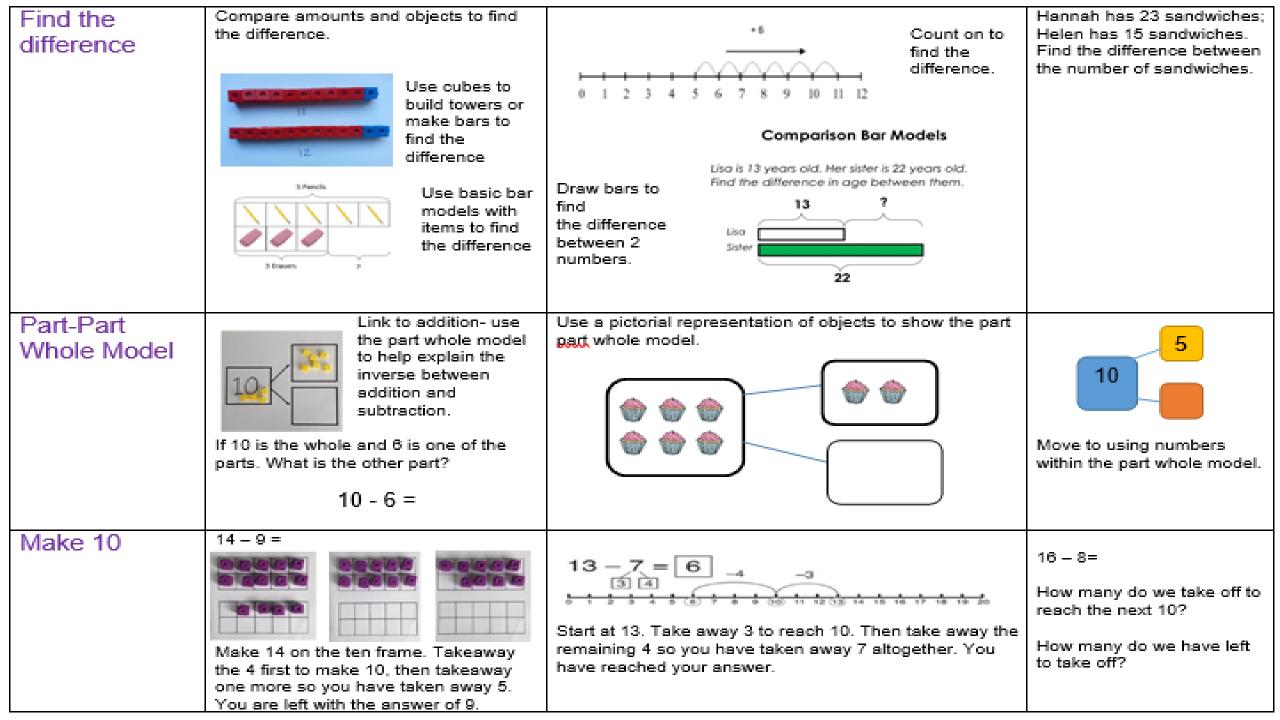
As the children move on, introduce decimals with the same number of decimal places and different. Money can be used here.  $\frac{+85}{621}$ 

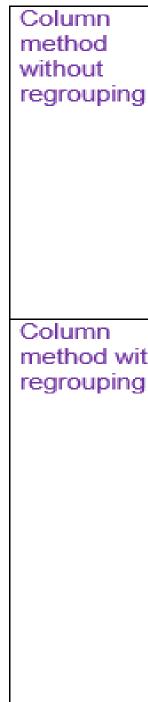
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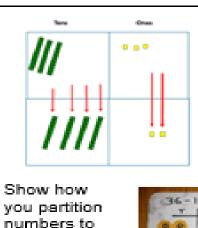




Subtraction			
Objective and	Concrete	Pictorial	Abstract
Strategies			
Taking away	Use physical objects, counters, cubes	Cross out drawn objects to show what has been taken away.	18 -3= 15
ones	etc. to show how objects can be taken away.		8 – 2 = 6
	6-2=4		
	4-2=2	15-3= 12	
	<b>→</b>		
Counting back	Make the larger number in your subtraction. Move the beads along your	Count back on a number line or number track	Put 13 in your head, count back 4. What number are
	bead string as you count backwards in ones.	9 10 11 12 13 14 15	you at? Use your fingers to help.
	13 – 4	Start at the bigger number and count back the smaller number showing the jumps on the number line.	
	Use counters and move them away		
	from the group as you take them away counting backwards as you go.	-10 -10	
		34 35 36 37 47 57	
		This can progress all the way to counting back using two 2 digit numbers.	





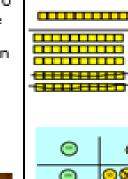


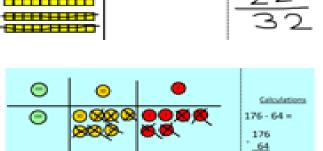
subtract. Again make the larger number first. Use Base 10 to make the bigger number then take the smaller. number away.

Calculations

- 88

234





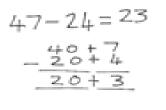
0088

10 or place value counters alongside the written. calculation to help to show working.

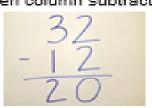
Draw the Base

Calculations

312



This will lead to a clear written column subtraction.





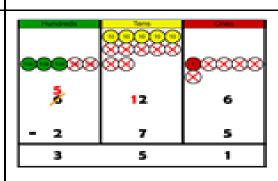
Use Base 10 to start with before moving on to place value counters. Start with one exchange before moving onto subtractions with 2 exchanges.

Make the larger number with the place value counters

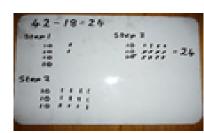
	0	•	Calculations
00	000	••••	234
Start wi	th the or	ies, can I take	away 8

from 4 easily? I need to exchange one of my tens for ten ones.

0	0	•
00	00	



Draw the counters onto a place value grid and show what you have taken away by crossing the counters out as well as clearly showing the exchanges you make.



When confident, children can find their own way to record the exchange/regrouping.

Just writing the numbers as shown here shows that the child understands the method

and knows when to exchange/regroup.



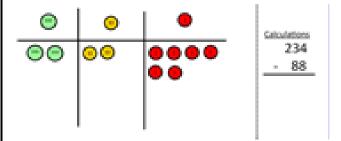
Children can start their formal written method by partitioning the number into clear place value columns.



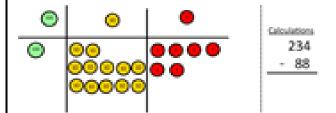
Moving forward the children use a more compact method.

Now I can subtract my ones.

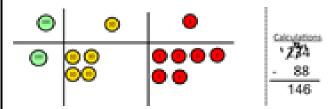
Now look at the tens, can I take away 8 tens easily? I need to exchange one hundred for ten tens.



Now I can take away eight tens and complete my subtraction

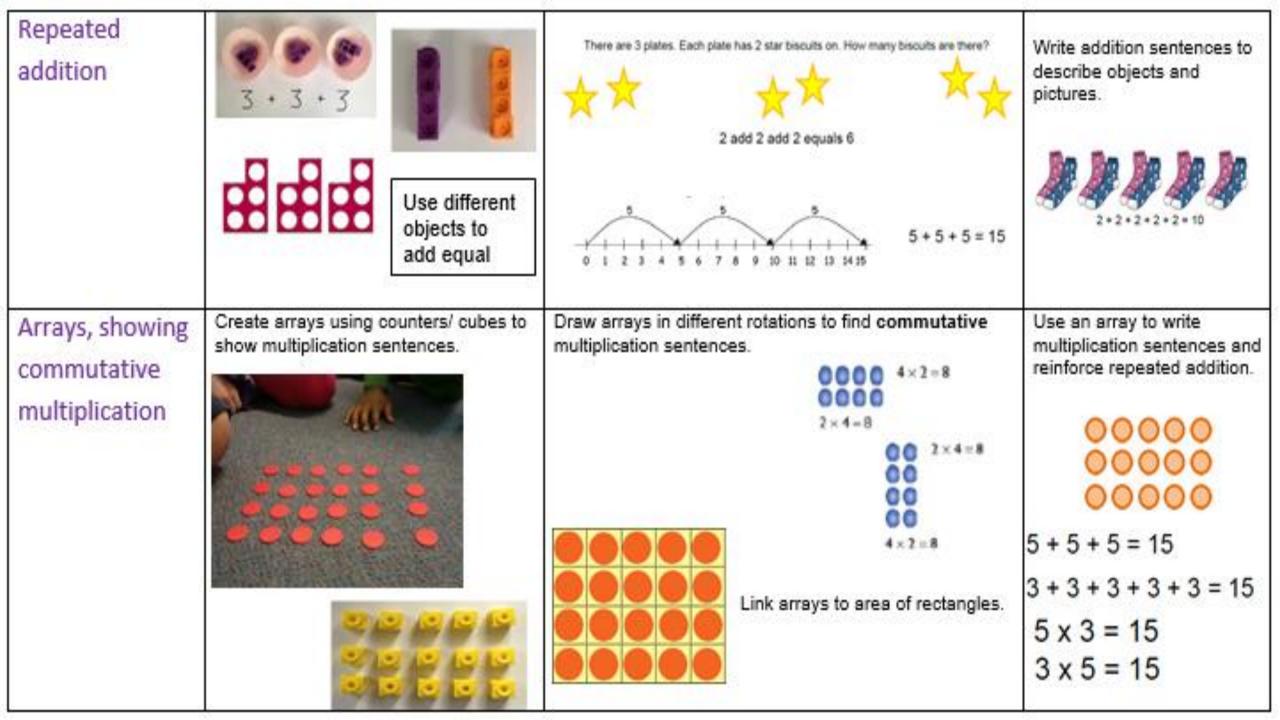


Show children how the concrete method links to the written method alongside your working. Cross out the numbers when exchanging and show where we write our new amount.



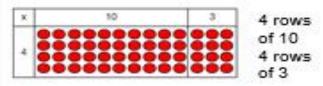
This will lead to an understanding of subtracting any number including decimals.

Multiplication Abstract Objective and Concrete Pictorial Strategies Use practical activities to show how to Doubling double a number. Draw pictures to show how to double a number. 16 Double 4 is 8 12 Partition a number and then double each part before double 4 is 8 recombining it back  $4 \times 2 = 8$ together. Count in multiples of a Counting in number aloud. multiples Write sequences with multiples of numbers. 2, 4, 6, 8, 10 5, 10, 15, 20, 25, 30 Use a number line or pictures to continue support in counting in multiples. Count in multiples supported by concrete objects in equal groups.

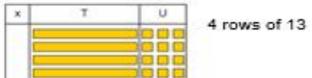




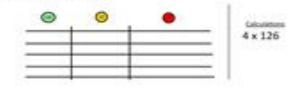
Show the link with arrays to first introduce the grid method.



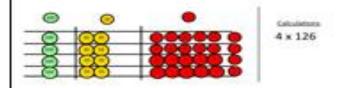
Move on to using Base 10 to move towards a more compact method.



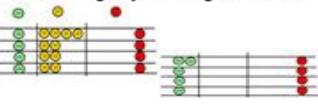
Move on to place value counters to show how we are finding groups of a number. We are multiplying by 4 so we need 4 rows.



Fill each row with 126.

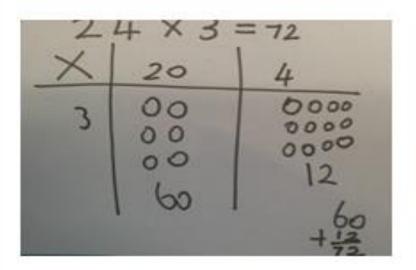


Add up each column, starting with the ones making any exchanges needed.



Children can represent the work they have done with place value counters in a way that they understand.

They can draw the counters, using colours to show different amounts or just use circles in the different columns to show their thinking as shown below.

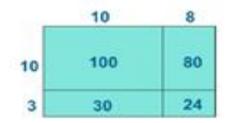


Start with multiplying by one digit numbers and showing the clear addition alongside the grid.

×	30	5
7	210	35

$$210 + 35 = 245$$

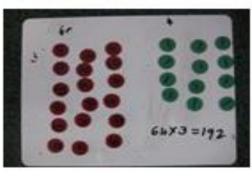
Moving forward, multiply by a 2 digit number showing the different rows within the grid method.



х	1000	300	40	2
10	10000	3000	400	20
8	8000	2400	320	16

Column
multiplication
100

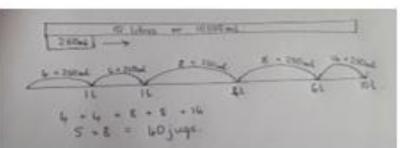
Children can continue to be supported by place value counters at the stage of multiplication.



It is important at this stage that they always multiply the ones first and note down their answer followed by the tens which they note below.

Bar modelling and number lines can support learners when solving problems with multiplication alongside the formal written methods.

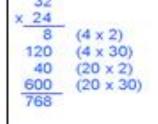




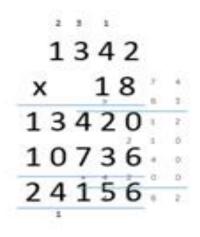
Start with long

multiplication, reminding the children about lining up their numbers clearly in columns.

If it helps, children can write out what they are solving next to their answer.

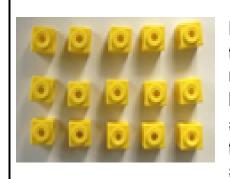


This moves to the more compact method.



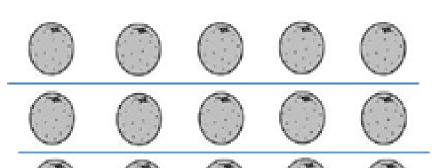
Division			
Objective and	Concrete	Pictorial	Abstract
Strategies			
Sharing objects	The second secon	Children use pictures or shapes to share quantities.	Share 9 buns between three people.
into groups		\$\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2	9 ÷ 3 = 3
	I have 10 cubes, can you share them equally in 2 groups?	\$\frac{1}{2} \frac{1}{2} \frac	
Division as	Divide quantities 1∩	Use a number line to show jumps in groups. The number	28 ÷ 7 = 4
grouping	into equal groups. Use cubes, counters, objects or place value counters to aid understanding.	of jumps equals the number of groups.  0 1 2 3 4 5 6 7 8 9 10 11 12  3 3 3 3 3	Divide 28 into 7 groups.  How many are in each group?
	96 + 3 = 32	Think of the bar as a whole. Split it into the number of groups you are dividing by and work out how many would be within each group.	
	• • • • • • • • • • • • • • • • • • •	<u> </u>	

### Division within arrays

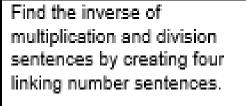


Link division to multiplication by creating an array and thinking about the

number sentences that can be created.

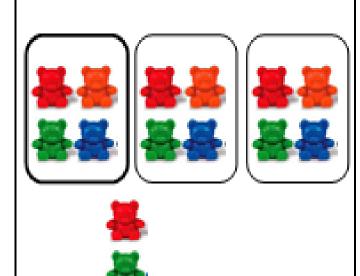


Draw an array and use lines to split the array into groups to make multiplication and division sentences.



#### Division with a remainder

14 ÷ 3 =
Divide objects between groups and see how much is left over



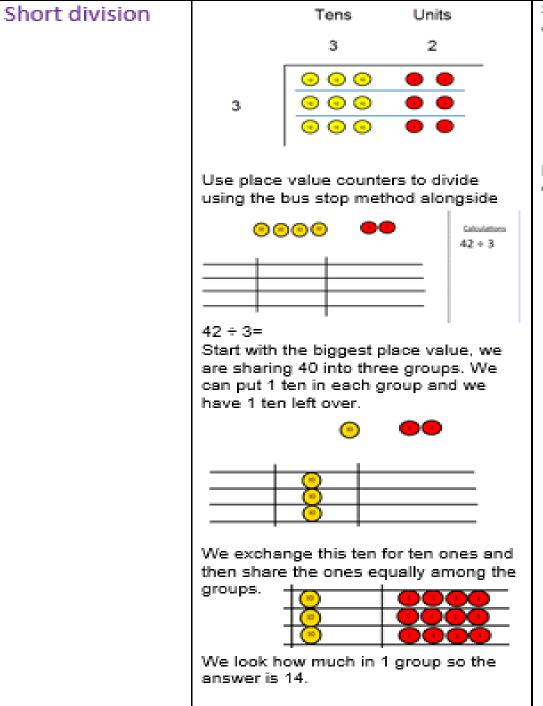
Jump forward in equal jumps on a number line then see how many more you need to jump to find a remainder.



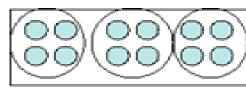
Draw dots and group them to divide an amount and clearly show a remainder.



Complete written divisions and show the remainder using r.

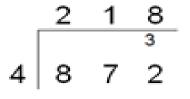


Students can continue to use drawn diagrams with dots or circles to help them divide numbers into equal groups.

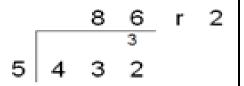


Encourage them to move towards counting in multiples to divide more efficiently.

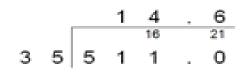
Begin with divisions that divide equally with no remainder.



Move onto divisions with a remainder.



Finally move into decimal places to divide the total accurately.



Children need to write their times table out on the right hand side of the page to support their calculations too.

02021		
U 3 X F 6		13
13 442 6 00		2 6
		3 9
		5 2
		5
		2 5
		1 1
	1 (	) 4

Number and calculation skills are the foundations that becoming numerate are built from pupils are taught to value a range of different strategies to work out number sentences and problems.

Through partner talk, questioning and discussion we would encourage pupils to find efficient methods.

There are countless mental strategies to use so throughout our teaching we are always asking pupils:

How did you work that at? What strategy did you use? Explain how you worked that out? Show me another way to work it out. Who found a different way to work it out? Which method would be the most efficient? I wonder what would happen if...? Prove it.

## WM 1 – THE NUMBER SYSTEM IS USED TO REPRESENT AND COMPARE RELATIONSHIPS BETWEEN NUMBERS AND QUANTITIES

Informal written recording will still take place regularly through methods. These are an important part of learning and understanding, where lots of discussion can occur around strategies being used and identify misconceptions and highlighting them at an early stage. More formal abstract methods follow only when the child is able to use a wide range of mental calculation strategies. The emphasis of our teaching will always be to facilitate understanding and not simply to arrive at a correct answer.

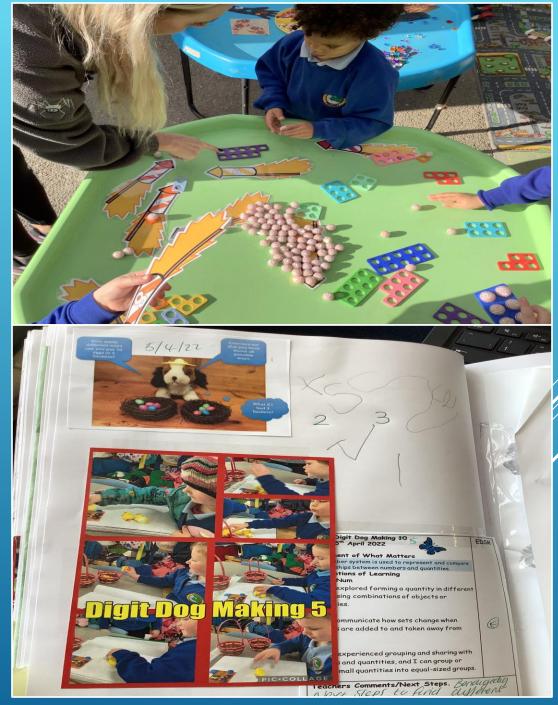
Pupils will always be encouraged to look at a calculation/problem and then decide, what is the best method to choose to solve the question? Our aim is for pupils to be able to select an efficient method of their choice (whether this be concrete, pictorial or abstract) that is appropriate for a given task. They will do this by asking themselves:

- Can I do this in my head? What facts do I need to use?
- What resources (concrete) in our learning environment might help me get to the answer?
- What pictures or drawings (pictorial) could I use to help see the 'maths journey'?
- What formal strategy (abstract) can I use to solve this?
- Will a calculator support this type of question better?

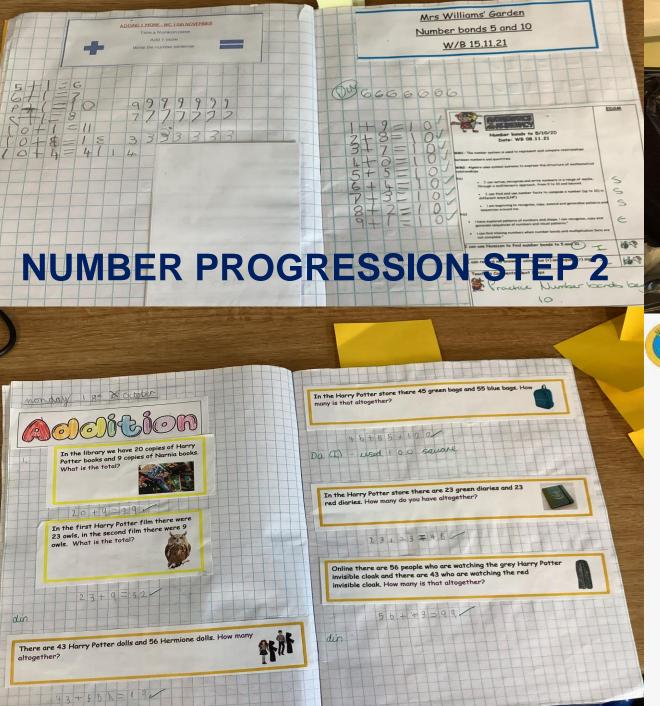
# WM 1 – THE NUMBER SYSTEM IS USED TO REPRESENT AND COMPARE RELATIONSHIPS BETWEEN NUMBERS AND QUANTITIES

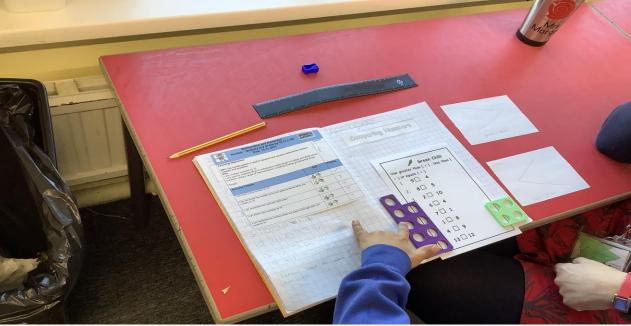
### NUMBER PROGRESSION STEP 1



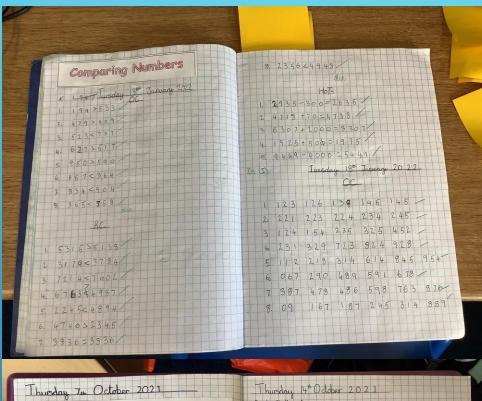












#### **Negative Numbers**

UF no need for prackets

- 1. 8 +(-5)=3
- 2. 9 + (- 3) = 6
- 3. 4+(-5)=(-1)
- 4. 2+(-4)=(-2)
- 5. (- 2)+(- 4)=(-6)
- 6. (-2)+(-1)=(-3) 7. (6+(-6):0
- 8. (-4)+(-5)=(-9)

Red Chilli A 1. 8 × (- 3) = (- 2 4) 1 8 × (-3) = - 2 4 2 24 -(-3)= -8 2 24 - (-3) = (-8) 4. (-40) - 2 = (-20) 4. (-40) + 2 = -2 5. 6 × (-7) = -42 5. 6 × (-7)=(-42) 8 (660 - (-12) = -5 9. (-9)×(-8)=72 Red Chille B 1 (-4) + 2 = -8 3 1(-12)×(-3)=36+ 4 (-48)+(-8)=-6 6. (-12)×(-6)=72

Red Chilli page 4 2 - B

1 1 2 3 4 5 6 7 8

1 1 2 8 1 12 16 20 24 28 32 Fractions 2 2 4 6 8 10 12 14 16 Mednesday 194 January 2022 1 = Halz 9 = Quarter 3 = Three quaters Red Chilli page 42-80 1 = Third 5 = Figh 1 = Whole 2 = 8 / 3 = 15 / 3 = 6 / 4 = 16 / 2 = 40 / 3 = 12 / 4 = 20 / 7 = 14 / 9 = 36 5 = 100 1 Berlin 2. Warsaw 3. Veinna 15 3 25 5 25 = 5 3 0 = 6 4. Athens Red Chilli page 42 A 1. 4 6.

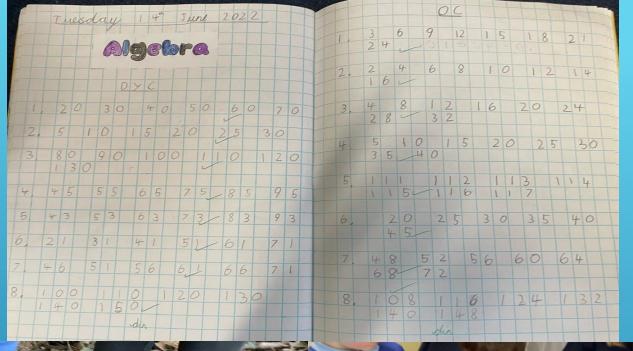
In Llanrhidian algebra is the study of structures abstracted from computations and relations, and provides a way to make generalisations. Algebraic thinking moves away from context to structure and relationships. This powerful approach provides our learners with the means to abstract important features and to detect and express mathematical structures of situations in order to solve problems. Algebra is a unifying thread running through the fabric of mathematics and numeracy.

Algebraic thinking is essential for reasoning, modelling and solving problems in mathematics and in a wide range of real-world contexts, including technology and finance. Making connections between arithmetic and algebra develops skills for abstract reasoning from as early as Pod Pila Pala.

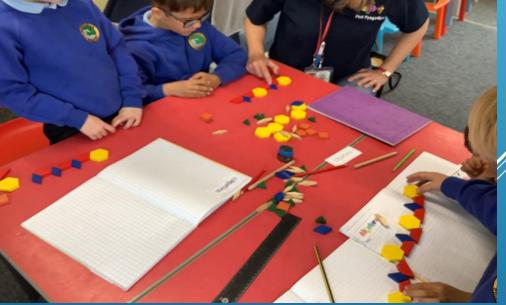
#### **ALGEBRA IN LLANRHIDIAN**



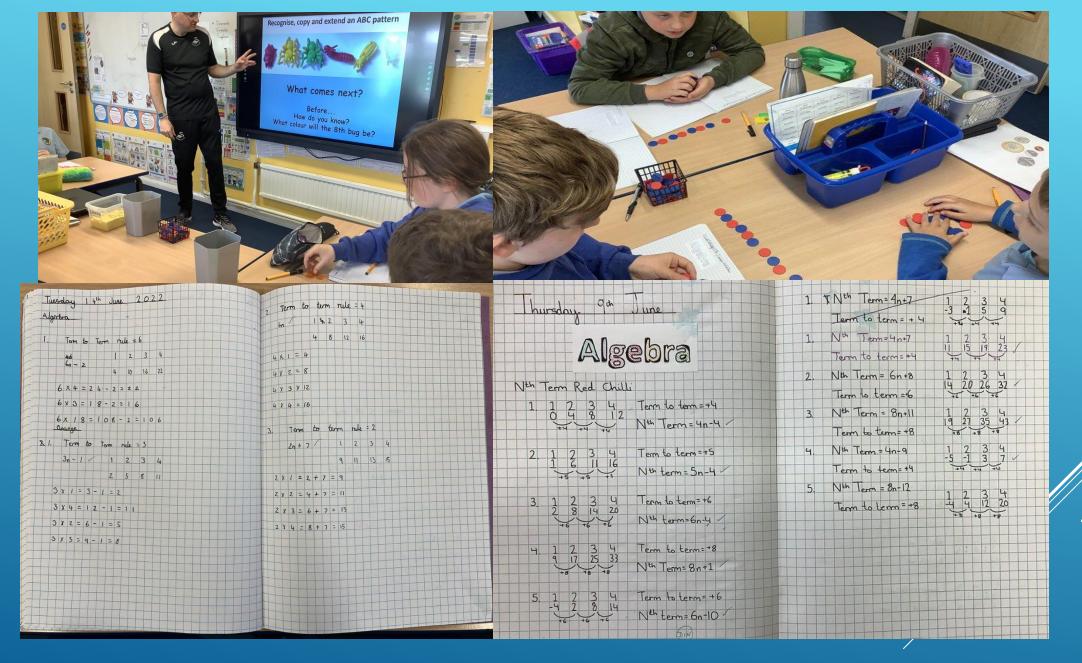
#### **ALGEBRA IN PROGRESSION STEP 1**







**ALGEBRA IN PROGRESSION STEP 2** 

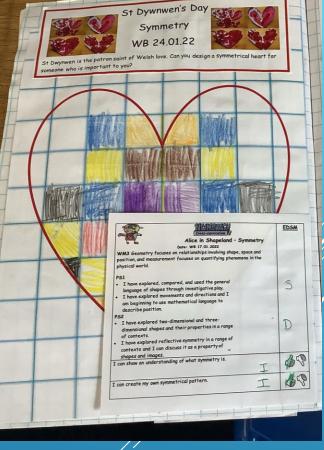


In Llanrhidian geometry involves playing with, manipulating, comparing, naming and classifying shapes and structures. The study of geometry encourages the development and use of conjecture, deductive reasoning and proof. Measurement allows the magnitude of spatial and abstract features to be quantified, using a variety of standard and non-standard units. It can also support the development of numerical reasoning for our learners.

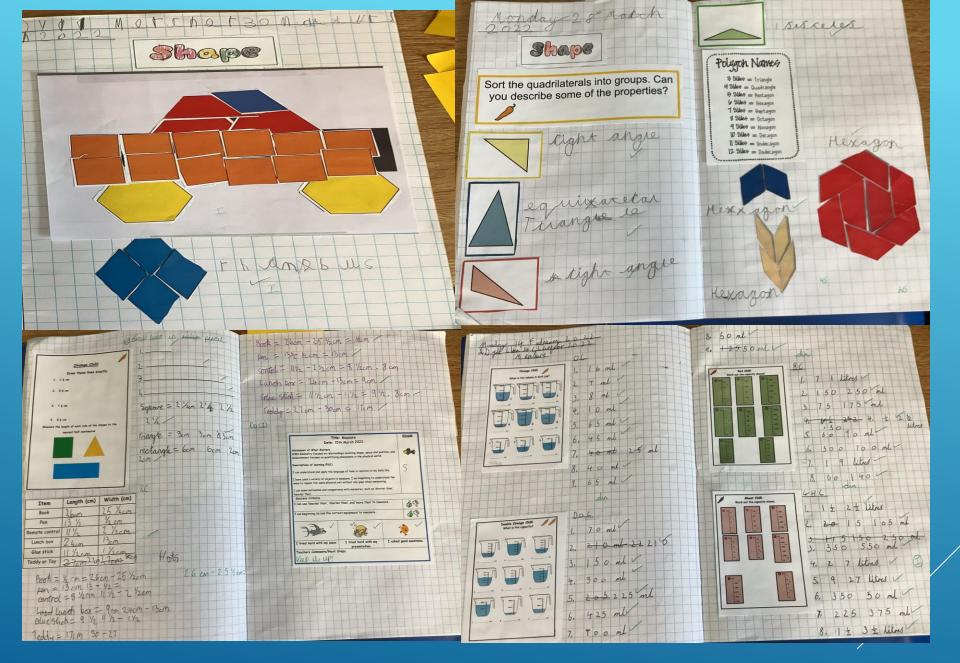
We value the importance of reasoning in Llanrhidian, reasoning about the sizes and properties of shapes and their surrounding spaces helps our learners to make sense of the physical world and the world of mathematical shapes. Geometry and measurement have applications in many fields, including art, construction, science and technology, engineering, and astronomy.

#### **GEOMETRY IN LLANRHIDIAN**

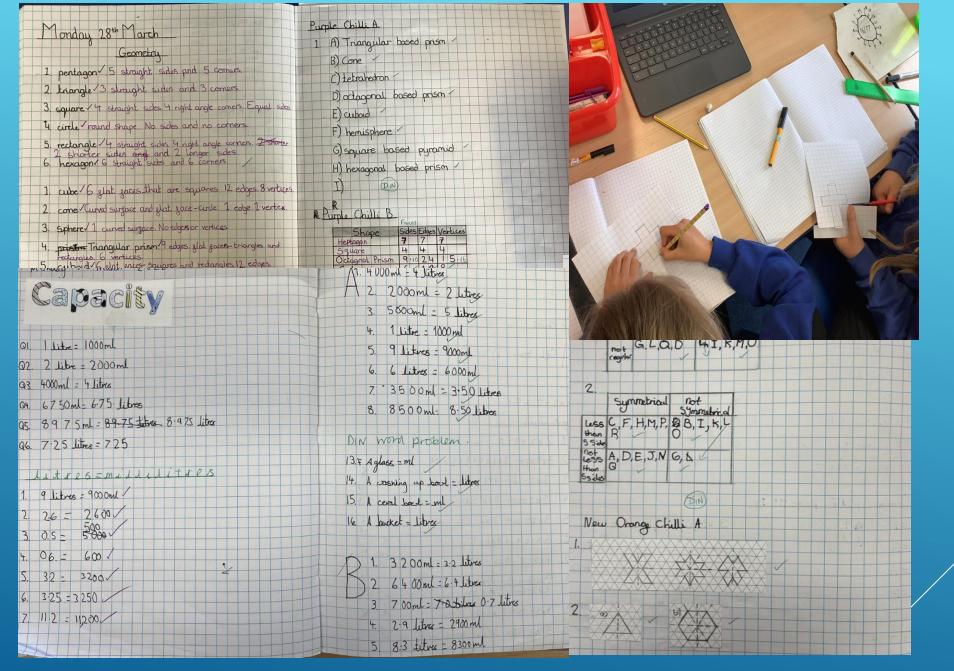




#### **GEOMETRY IN PROGRESSION 1**



**GEOMETRY IN PROGRESSION 2** 



In Llanrhidian statistics is the practice of collecting, manipulating and analysing data, allowing representation and generalisation of information. Probability is the mathematical study of chance, enabling predictions of the likelihood of events occurring. Statistics and probability rely on the application and manipulation of number and algebra. The process of reasoning with statistics and probability, and evaluating their reliability, develops critical thinking and analytical skills that are fundamental to enabling our learners to make ethical and informed decisions.

#### Data

In Llanrhidian managing data and representing information effectively provide our learners with the means to test hypotheses, draw conclusions and make predictions.

- •Describing data Reading data from graphs, tables, lists
- Organising data Ordering, grouping, summarising
- Representing data Labelling, scaling
- Analysing data Making inferences, predictions, interpreting patterns and trends

In Llanrhidian there is a progression of graphs, which includes:

Real graphs - object graphs - a small step from classification.

Picture graphs – pictograms – The picture can represent one piece of data

Symbolic graphs – bar charts and line graphs.

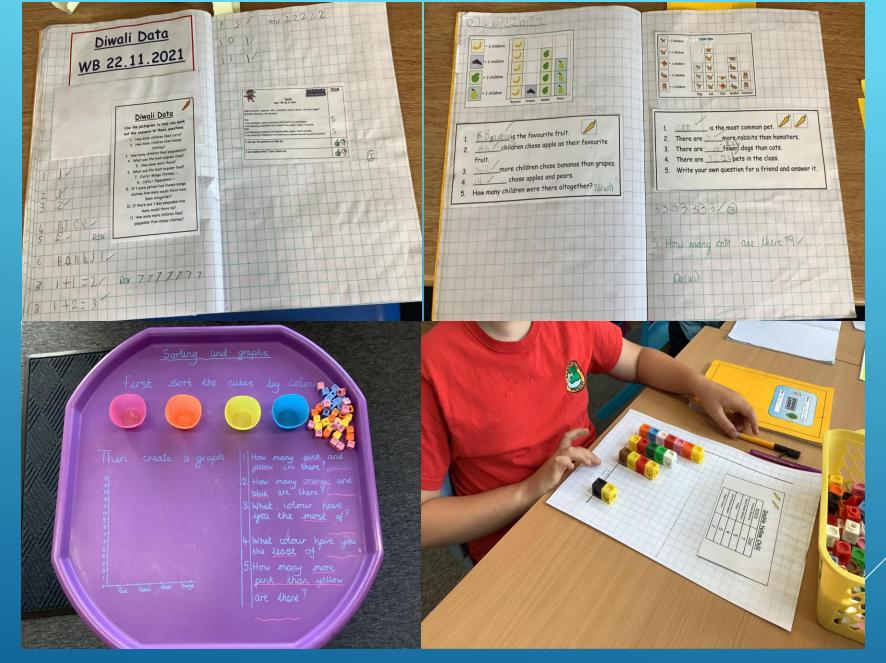
#### Classification

Classification happens right from Pila – Pala to Pry Cop. In Llanrhidian in order to formulate questions and decide how to represent data that has been gathered, decisions must be made about how things might be categorised. Our learners have lots of varied opportunities to sort and classify and talk about how they have done this i.e. sorting shapes, sorting hair colour and eye colour or sorting responses to big questions.

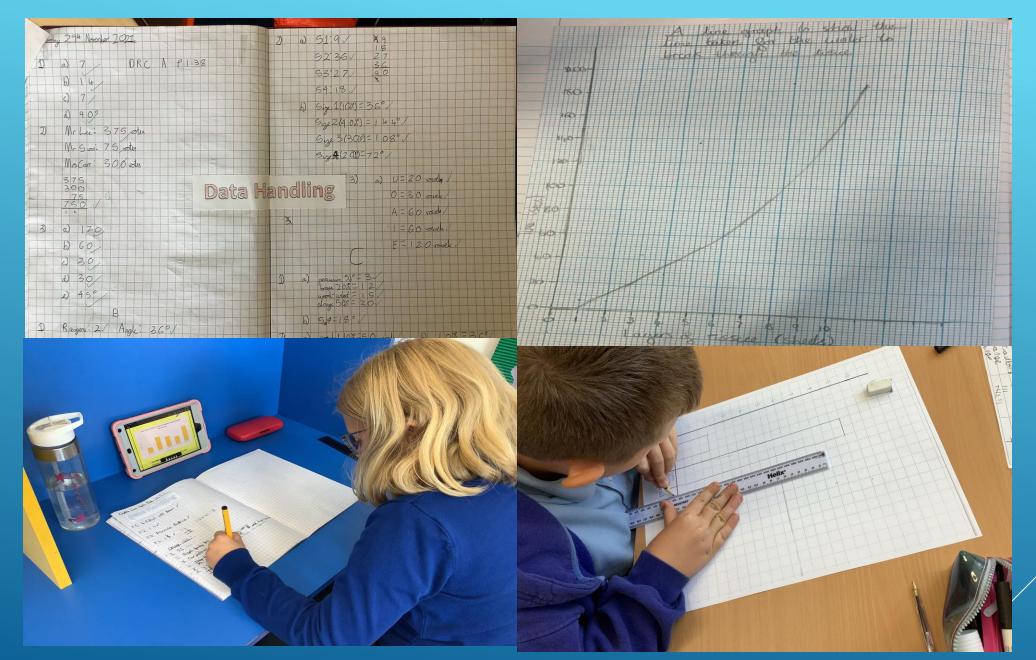
#### STATISTICS AND DATA IN LLANRHIDIAN



#### **DATA HANDLING IN PROGRESSION 1**



**DATA HANDLING IN PROGRESSION 2** 



**DATA HANDLING IN PROGRESSION 3**